

# **CS 106**

# **INTRODUCTION TO**

# **DATA STRUCTURES**

**SPRING 2020**

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**HVERFORD COLLEGE**

# ADMIN

- **Lab 1 due TOMORROW**
- **Lab 2 due next Wednesday**
- **Before lab on Friday, mostly complete with the pre-lab (okay to finish in lab)**
- **Office Hours TODAY 4:30-6pm (H110)**
- **Review quiz will be collected on Thursday**
  - Full credit for putting your name and answering one question (does not have to be correct!)
  - On the material from today

# **FEB 11 OUTLINE**

- **Digital Scholars program**
- **StringBuilder**
- **Begin: runtime analysis**
- **Recap ArrayLists and Generics**
- **Begin: Singly Linked Lists**

# FEB 11 OUTLINE

- Digital Scholars program
- **StringBuilder**
- Begin: runtime analysis
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# STRING BUILDER

Since Strings are immutable, any change to the reference means a new copy has to be created!

```
String greeting = "hello";  
greeting += "!";  
System.out.println(greeting);
```

# STRING BUILDER

Since Strings are immutable, any change to the reference means a new copy has to be created!

```
String greeting = "hello";  
greeting += "!";  
System.out.println(greeting);
```

StringBuilder provides a way of creating a mutable String.

```
StringBuilder sb = new StringBuilder("Hello");  
sb.append("!");  
sb.setCharAt(0, 'M');  
sb.insert(4, "oooo");  
System.out.println(sb);
```

# STRING BUILDER

Since Strings are immutable, any change to the reference means a new copy has to be created!

```
String greeting = "hello";  
greeting += "!";  
System.out.println(greeting);
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StringBuilder provides a way of creating a mutable String.

```
StringBuilder sb = new StringBuilder("Hello");  
sb.append("!");  
sb.setCharAt(0, 'M');  
sb.insert(4, "oooo");  
System.out.println(sb);
```

Output: "Mellooooo!"

```
public class PersonList {
```

```
    public String toString() {  
        StringBuilder sb  
        for loop
```

```
        return Sb.toString();  
    }  
}
```

wrong type

main

```
PersonList ml  
System.out.println(ml);
```



# FEB 11 OUTLINE

- Digital Scholars program
- StringBuilder
- **Begin: runtime analysis**
- Recap ArrayLists and Generics
- Begin: Singly Linked Lists

# RUNTIME: HANDOUT 7, PG 1

```
1. n = int(input("n: "))  
   for i in range(n):  
       print(i)
```

# RUNTIME: HANDOUT 7, PG 1

```
1. n = int(input("n: "))  
   for i in range(n):  
       print(i)
```

$n$  steps  $\Rightarrow O(n)$

*linear*

```
2. n = int(input("n: "))  
   for i in range(100):  
       print(i*n)
```

# RUNTIME: HANDOUT 7, PG 1

```
1. n = int(input("n: "))  
   for i in range(n):  
       print(i)
```

$n$  steps  $\Rightarrow O(n)$

*linear*

```
2. n = int(input("n: "))  
   for i in range(100):  
       print(i*n)
```

100 steps  $\Rightarrow O(1)$

*constant*

```
3. n = int(input("n: "))  
   for i in range(n):  
       print(i)  
   for j in range(n):  
       print(j)
```

# RUNTIME: HANDOUT 7, PG 1

```
1. n = int(input("n: "))  
   for i in range(n):  
       print(i)
```

$n$  steps  $\Rightarrow O(n)$

*linear*

```
2. n = int(input("n: "))  
   for i in range(100):  
       print(i*n)
```

100 steps  $\Rightarrow O(1)$

*constant*

```
3. n = int(input("n: "))  
   for i in range(n):  
       print(i)  
   for j in range(n):  
       print(j)
```

$2n$  steps  $\Rightarrow O(n)$

*linear*

# RUNTIME: HANDOUT 7, PG 1

```
4. n = int(input("n: "))
   for i in range(n):
       for j in range(n):
           print(i, j)
```

# RUNTIME: HANDOUT 7, PG 1

```
4. n = int(input("n: "))
   for i in range(n):
       for j in range(n):
           print(i, j)
```

$n^2$  steps  $\Rightarrow O(n^2)$

*quadratic*

```
5. n = int(input("n: "))
   for i in range(n):
       for j in range(i,n):
           print(i, j)
```

# RUNTIME: HANDOUT 7, PG 1

```
4. n = int(input("n: "))
   for i in range(n):
       for j in range(n):
           print(i, j)
```

$n^2$  steps  $\Rightarrow O(n^2)$

*quadratic*

```
5. n = int(input("n: "))
   for i in range(n):
       for j in range(i, n):
           print(i, j)
```

$n^2/2$  steps  $\Rightarrow O(n^2)$

*quadratic*

```
6. n = int(input("n: "))
   for i in range(n):
       for j in range(10):
           print(i, j)
```



# RUNTIME: HANDOUT 7, PG 1

```
4. n = int(input("n: "))  
   for i in range(n):  
       for j in range(n):  
           print(i, j)
```

$n^2$  steps  $\Rightarrow O(n^2)$

*quadratic*

```
5. n = int(input("n: "))  
   for i in range(n):  
       for j in range(i, n):  
           print(i, j)
```

$n^2/2$  steps  $\Rightarrow O(n^2)$

*quadratic*

```
6. n = int(input("n: "))  
   for i in range(n):  
       for j in range(10):  
           print(i, j)
```

$10n$  steps  $\Rightarrow O(n)$

*linear*

# RUNTIME: HANDOUT 7, PG 1

```
7. n = int(input("n: "))
   while n > 1:
       print(n)
       n = n/2
```

# RUNTIME: HANDOUT 7, PG 1

```
7. n = int(input("n: "))
   while n > 1:
       print(n)
       n = n/2
```

$\log(n)$  steps  $\Rightarrow O(\log(n))$

*logarithmic*

```
8. arraylst = {1,2,5,7,13,21,24,25,26,33,34,38,50,57,58,63}
   n = arraylst.length
   mid = int(n/2)
   print lst[mid]
```

# RUNTIME: HANDOUT 7, PG 1

```
7. n = int(input("n: "))
   while n > 1:
       print(n)
       n = n/2
```

$\log(n)$  steps  $\Rightarrow O(\log(n))$

*logarithmic*

```
8. arraylst = {1,2,5,7,13,21,24,25,26,33,34,38,50,57,58,63}
   n = arraylst.length
   mid = int(n/2)
   print lst[mid]
```

3 steps  $\Rightarrow O(1)$

*constant*

```
9. n = int(input("n: "))
   for i in range(n):
       k = n
       while k > 1:
           print(i, k)
           k = k/2
```

# RUNTIME: HANDOUT 7, PG 1

```
7. n = int(input("n: "))
   while n > 1:
       print(n)
       n = n/2
```

$\log(n)$  steps  $\Rightarrow O(\log(n))$

*logarithmic*

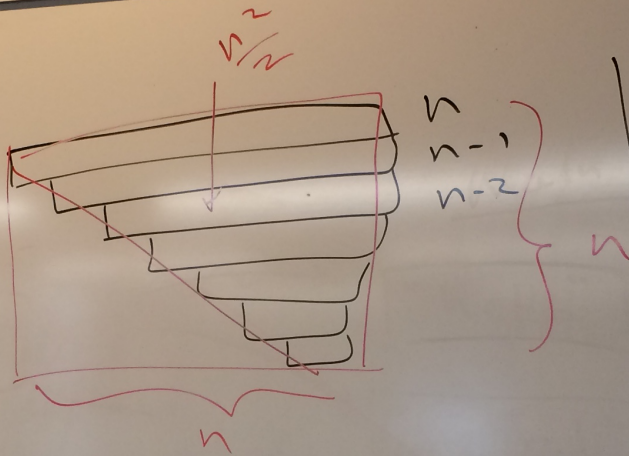
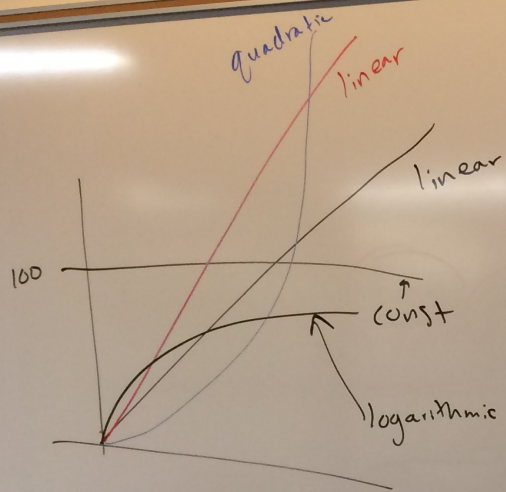
```
8. arraylst = {1,2,5,7,13,21,24,25,26,33,34,38,50,57,58,63}
   n = arraylst.length
   mid = int(n/2)
   print lst[mid]
```

3 steps  $\Rightarrow O(1)$

*constant*

```
9. n = int(input("n: "))
   for i in range(n):
       k = n
       while k > 1:
           print(i, k)
           k = k/2
```

$n \log(n)$  steps  $\Rightarrow O(n \log(n))$



$$n + (n-1) + \dots + 2 + 1 = S$$

$$\frac{n(n+1)}{2}$$

log

$$\frac{n}{2^x} = 1$$

$$\log(n) = \log(2^x)$$

$$x = \log(n)$$

# FEB 11 OUTLINE

- Digital Scholars program
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- Begin: runtime analysis
- **Recap ArrayLists and Generics**
- Begin: Singly Linked Lists

# ARRAYLISTS: INITIALIZATION

```
import java.util.ArrayList;
```

Imports the library for the ArrayList class.

```
ArrayList<String> myList = new ArrayList<String>();
```

The type that the underlying array will be declared to have. These are known as generics in Java.

No need to give a specific length!

**Source code for the class:**

```
public class ArrayList<T> {  
    private T[] dataArray;
```

```
...
```

This is how classes with generic types are created and then used.



# LAST TIME

- Wrote our own `ArrayList` class!
- Implemented the “add” method

```
public void add(T elem) {
    int l = array.length;

    // no more space: resize
    if (numElem == l) {
        T[] arrayNew = (T[]) new Object[l*2];
        for (int i=0; i < l; i++) {
            arrayNew[i] = array[i];
        }
        array = arrayNew;
    }

    // add new element
    array[ numElem ] = elem;
    numElem++;
}
```

# LAST TIME

- Wrote our own `ArrayList` class!
- Implemented the “add” method

```
public void add(T elem) {
    int l = array.length;

    // no more space: resize
    if (numElem == l) {
        T[] arrayNew = (T[]) new Object[l*2];
        for (int i=0; i < l; i++) {
            arrayNew[i] = array[i];
        }
        array = arrayNew; // update reference
    }

    // add new element
    array[numElem] = elem;
    numElem += 1;
}
```

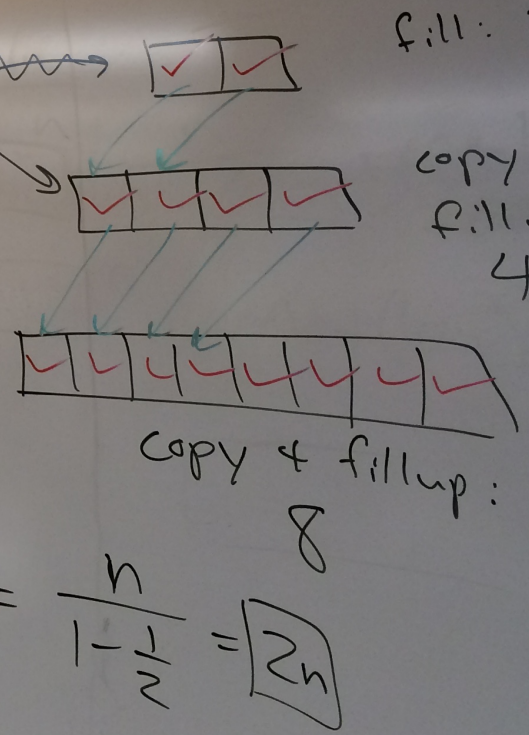
Why is adding an element to the end of an ArrayList  $O(1)$  on average?

initial space =  $a$   
 scaling factor =  $r$   
 Example:  $a=2$   
 $r=2$

Q: how much work to get to size  $n$ ?

generic  
 runtime:  
 $n \left( \frac{1}{1 - \frac{1}{r}} \right)$   
 constant  
 $\Rightarrow$  linear

$$\begin{aligned} \text{runtime} &= 2 + 4 + 8 + 16 + 32 + \dots + n \\ &= 2 \left( 1 + \frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \dots + \frac{2}{n} \right) \\ &= 2 \left( \underbrace{1 + \frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \dots + \frac{2}{n}}_{\text{geometric series}} \right) \end{aligned}$$



$$= \frac{n}{1 - \frac{1}{2}} = 2n$$

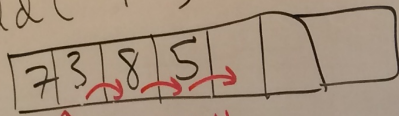
# Handout 7: Page 2

Do the rest on your own!

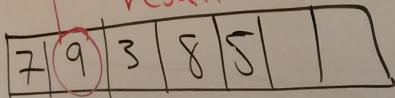
① add:  $O(1)$  on average

② add(*<index>*, *<element>*)  
add(1, 9)

how can we do better?



result

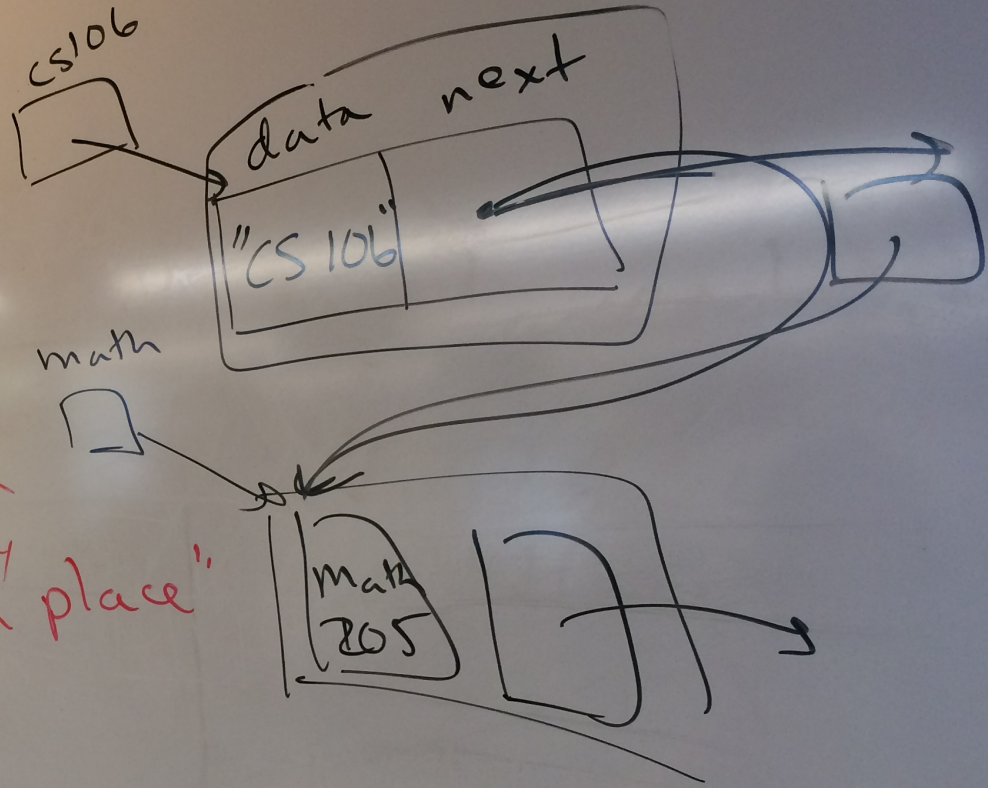


not a copy  
"in place"

$O(n)$  worst case

③  $O(1)$  always

get(2)  $\Rightarrow$  2



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- **Begin: Singly Linked Lists**

# SINGLY LINKED LISTS

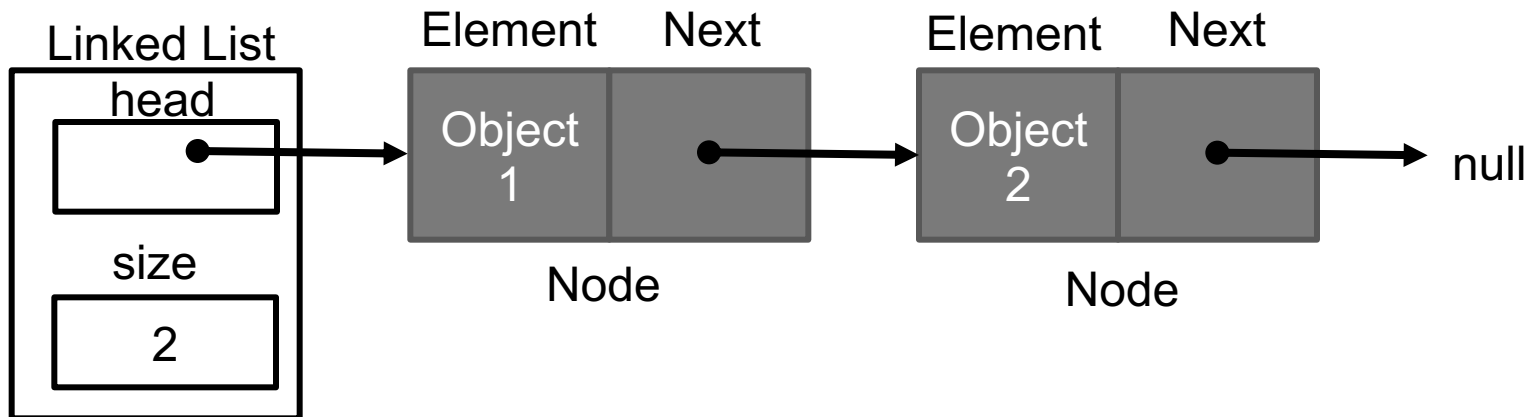
**Arrays and ArrayLists need to do work to store more items than anticipated.**

**What if we want our list storage to grow and shrink quickly and only store as much as we're using?**

**We can use a linked list! Every item stores a pointer to the next item.**

# SINGLY LINKED LISTS

Singly Linked Lists store items in order in a list by storing the head and size of the list. Each item (Node) then stores a pointer to the next item.



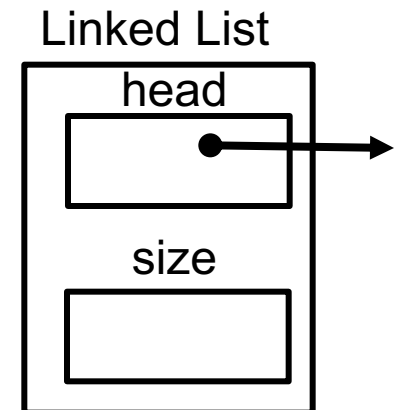
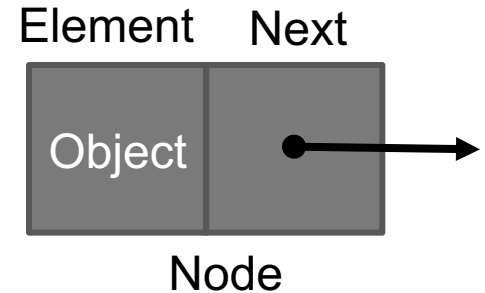
# CODING EXERCISE

Make a Node class that can be used as part of a Linked List:

1. Make a Node class that takes a generic type E
2. Add the relevant private fields to the Node class
3. Add a constructor that takes these fields as input
4. Add needed getters and setters

Make a LinkedList class:

1. Add and initialize needed instance variables
2. Make a constructor that takes no input



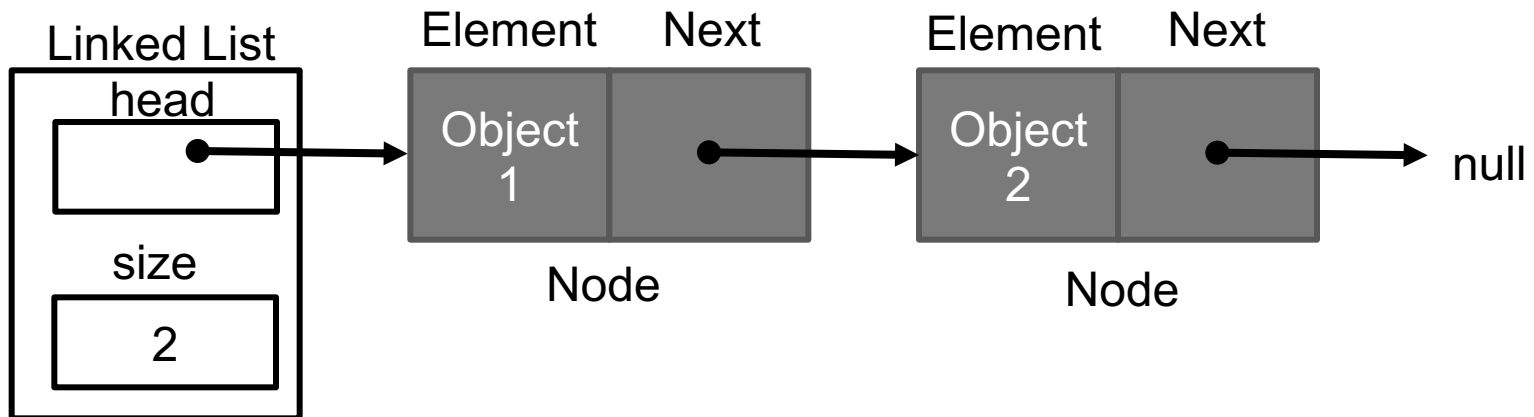


# TRAVERSING A LINKED LIST

start at the head pointer and let the current node = head

while the current node is not null

- get the element
- let the current node = next

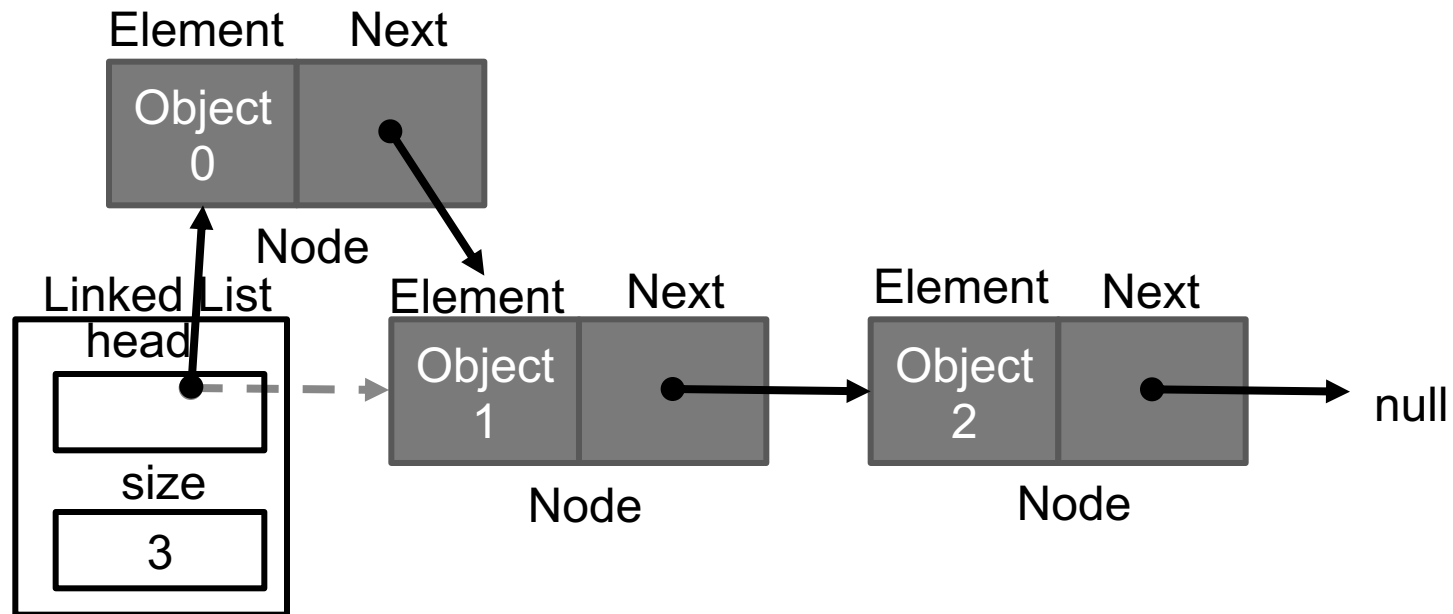


# ADDING AN ELEMENT (AT THE HEAD)

Create the Node and set a next pointer equal to head

Let head point to the created Node

Add 1 to the size



# ADDING AN ELEMENT (NOT AT THE HEAD)

Traverse the list until the Node before the one being added

*Slow!*

Create a new Node, link it to the Node that will come after it in the list, and point to it from the Node before it

Add 1 to the size

