

**Naive Bayes (continued)**

*(find and work with a partner)*

- Continuing the example from Handout 11, say we have a new data point  $\mathbf{x}_{\text{test}} = [\text{neg}, \text{pos}]$ . Our goal is to predict the class label based on the Naive Bayes posterior probability. In practice, we will compute this probability for each class  $k$ , based on our estimates ( $\theta_k$  and  $\theta_{k,j,v}$  terms). Then we will assign this data point the class label with maximum probability:

$$\hat{y} = \arg \max_{k \in \{1, 2, \dots, K\}} p(y = k | \mathbf{x}) = \arg \max_{k \in \{1, 2, \dots, K\}} p(y = k) \prod_{j=1}^p p(x_j | y = k).$$

For this  $\mathbf{x}_{\text{test}}$ , compute  $p(y = 1 | \mathbf{x}_{\text{test}})$  and  $p(y = 2 | \mathbf{x}_{\text{test}})$  and then assign a prediction label  $\hat{y}$ .

- For the tennis example below, fill in the  $\theta_{k,j,v}$  terms (thinking about how this could be implemented using dictionaries).

Day	Outlook	Temperature	Humidity	Wind	PlayTennis ( $y$ )
$\mathbf{x}_1$	Sunny	Hot	High	Weak	No
$\mathbf{x}_2$	Sunny	Hot	High	Strong	No
$\mathbf{x}_3$	Overcast	Hot	High	Weak	Yes
$\mathbf{x}_4$	Rain	Mild	High	Weak	Yes
$\mathbf{x}_5$	Rain	Cool	Normal	Weak	Yes
$\mathbf{x}_6$	Rain	Cool	Normal	Strong	No
$\mathbf{x}_7$	Overcast	Cool	Normal	Strong	Yes
$\mathbf{x}_8$	Sunny	Mild	High	Weak	No
$\mathbf{x}_9$	Sunny	Cool	Normal	Weak	Yes
$\mathbf{x}_{10}$	Rain	Mild	Normal	Weak	Yes
$\mathbf{x}_{11}$	Sunny	Mild	Normal	Strong	Yes
$\mathbf{x}_{12}$	Overcast	Mild	High	Strong	Yes
$\mathbf{x}_{13}$	Overcast	Hot	Normal	Weak	Yes
$\mathbf{x}_{14}$	Rain	Mild	High	Strong	No

**y=No (0)**

outlook	<b>Sunny:</b>	<b>Overcast:</b>	<b>Rain:</b>
temperature	<b>Cool:</b>	<b>Mild:</b>	<b>Hot:</b>
humidity	<b>Normal:</b>	<b>High:</b>	
wind	<b>Weak:</b>	<b>Strong:</b>	

**y=Yes (1)**

outlook	<b>Sunny:</b>	<b>Overcast:</b>	<b>Rain:</b>
temperature	<b>Cool:</b>	<b>Mild:</b>	<b>Hot:</b>
humidity	<b>Normal:</b>	<b>High:</b>	
wind	<b>Weak:</b>	<b>Strong:</b>	