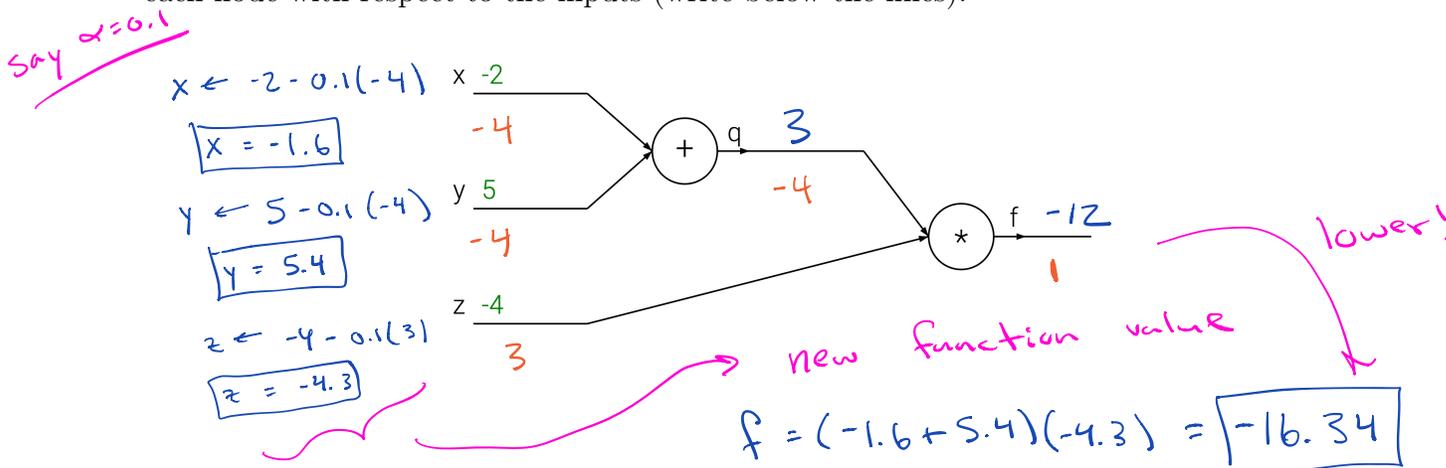


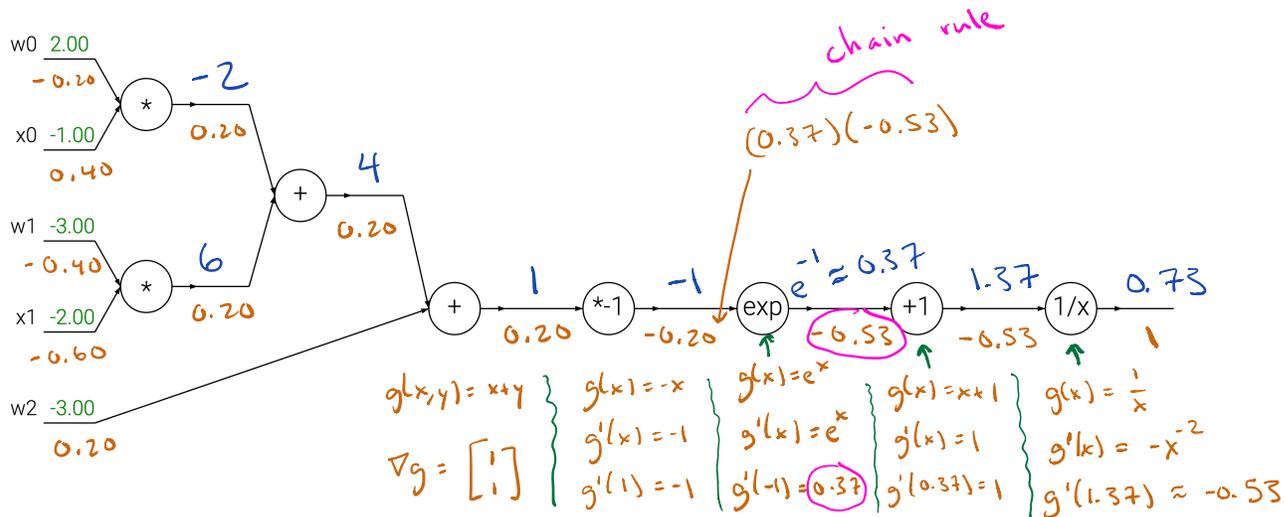
Backpropagation

— gradient
 — node value (find and work with a partner)

- Let $f(x, y, z) = (x + y)z$, a function of three inputs. Let $q = x + y$, so we can rewrite this function as $f = qz$. To determine how f changes as each input changes, we will use backpropagation through this neural network. First run the “forward pass” to compute the output value of each node (write above the lines). Then use the idea of the chain rule to compute the derivative of each node with respect to the inputs (write below the lines).



- Let $f(w_0, w_1, w_2, x_0, x_1) = \frac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$. Again compute the forward pass (can use a calculator) to determine the output value of each node, then use backpropagation to determine the gradients.



- Let $f(a, b, c, d) = (3a - b)^2 + cd$, a function of four inputs. We could decompose the function into a neural network diagram in many ways, but one way is shown below. Using the given values, first run the “forward pass” to compute the output value of each node (write above the lines). Then use backpropagation to compute the derivatives (write below the lines). If we wanted to minimize f with respect to these inputs and we have a learning rate of $\alpha = 0.1$, what values of a, b, c, d would we choose for the next step?

