



# CS 68: BIOINFORMATICS

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# Outline: Feb 5

- Global sequence alignment (Needleman-Wunsch)
- Dynamic Programming table + traceback

## Notes:

- Office hours today 3-5pm

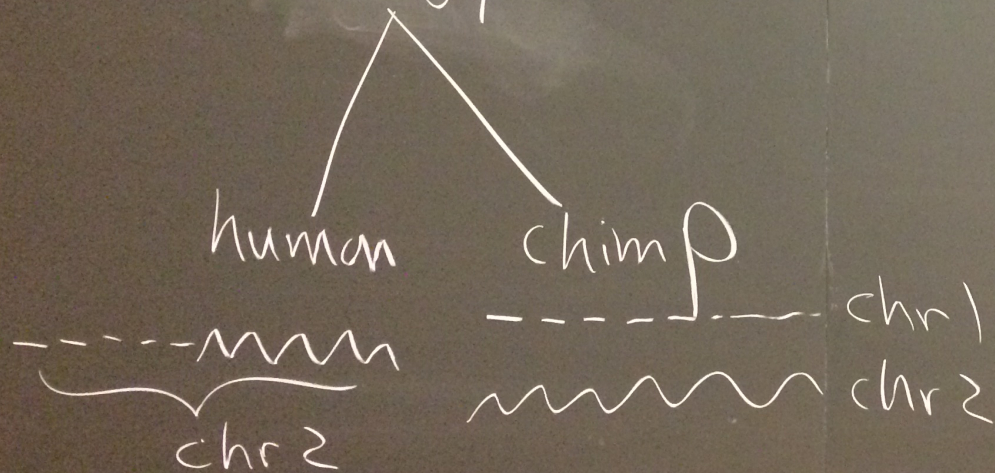
# Sequence Alginment

# Sequence Alignment

Why? understand evolution

↳ natural selection

↳ homology

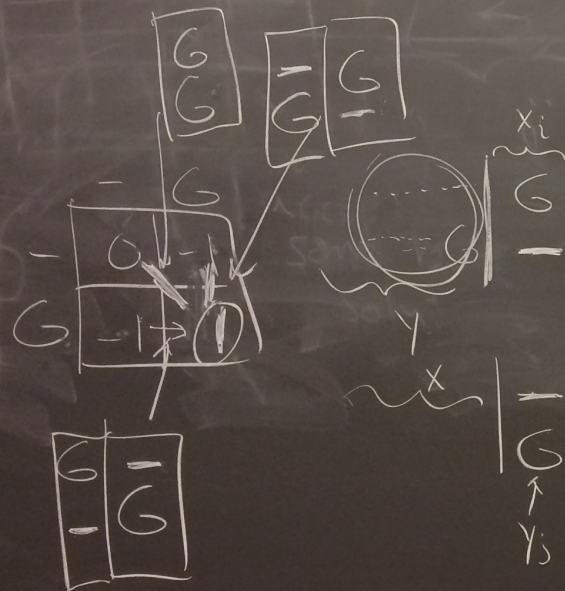


## ways seq can change

- ① substitution / mutation
- ② insertion } gaps
- ③ deletions }



$$m(a,b) = \begin{cases} 1 & \text{if } a=b \\ -1 & \text{o.w.} \end{cases}$$



len  $\begin{cases} n=4 \\ m=3 \end{cases}$   $\begin{cases} x = \overline{AAAC} \\ y = \overline{AGC} \end{cases}$   
 $\begin{matrix} x_1 & x_2 & x_3 & x_4 \\ y_1 & y_2 & y_3 \end{matrix}$

$s(3,2)$   $\begin{cases} \dots A \} \text{gap in } y \\ \dots - \} \end{cases}$   
 $\begin{cases} \dots - \} \text{gap in } x \\ \dots G \} \end{cases}$   
 $\begin{cases} \dots A \} \text{match score} \\ \dots G \} \end{cases}$

$\begin{cases} \text{match} = +1 \\ \text{mismatch} = -1 \\ \text{gap } g = -2 \end{cases}$



DP table

A      G      C

A

A

A

C

0	-2	-4	-6
-2	1	-1	-3
-4	-1	0	-2
-6	-3	-2	-1
-8	-5	-4	-1

base case

base case

recursive

$$s(i, j) = \max \begin{cases} s(i-1, j) + g \\ s(i, j-1) + g \\ s(i-1, j-1) + m(x_i, y_j) \end{cases}$$

$$s(n, m) = s(x, y)$$

Overall best alignment score

$$s(2, 2) = \max \begin{cases} s(1, 2) \\ s(2, 1) \\ s(1, 1) \end{cases}$$



$$s(i-1, j) + g$$

$$s(i, j-1) + g$$

$$s(i-1, j-1) + m(x_i, y_j)$$

Interpretation

\* Score is positive:

→ seqs are related

\* Score is negative

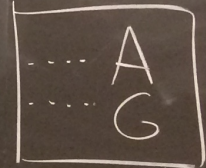
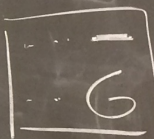
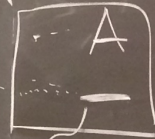
→ seqs are unrelated

$$s(x, y)$$

$$s(2, 2) = \max \begin{cases} s(1, 2) + g = -1 - 2 = -3 \\ s(2, 1) + g = -1 - 2 = -3 \\ s(1, 1) + m(A, G) = 1 + (-1) = 0 \end{cases}$$

align  
x<sub>i</sub>  
with  
gap

align y<sub>j</sub> with gap



all of y



find alignment

- Start at  $s(m, m)$
- go back to cell(s) that produced best alignment

11 of 4

next

action

A	A	A	C
-	A	G	C

↙

A	A	A	C
A	G	-	C

A	A	A	C
A	-	G	C