

# CSC 334: TOPICS IN COMPUTATIONAL BIOLOGY

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“Algorithms for Genomic Data”

Fall 2015

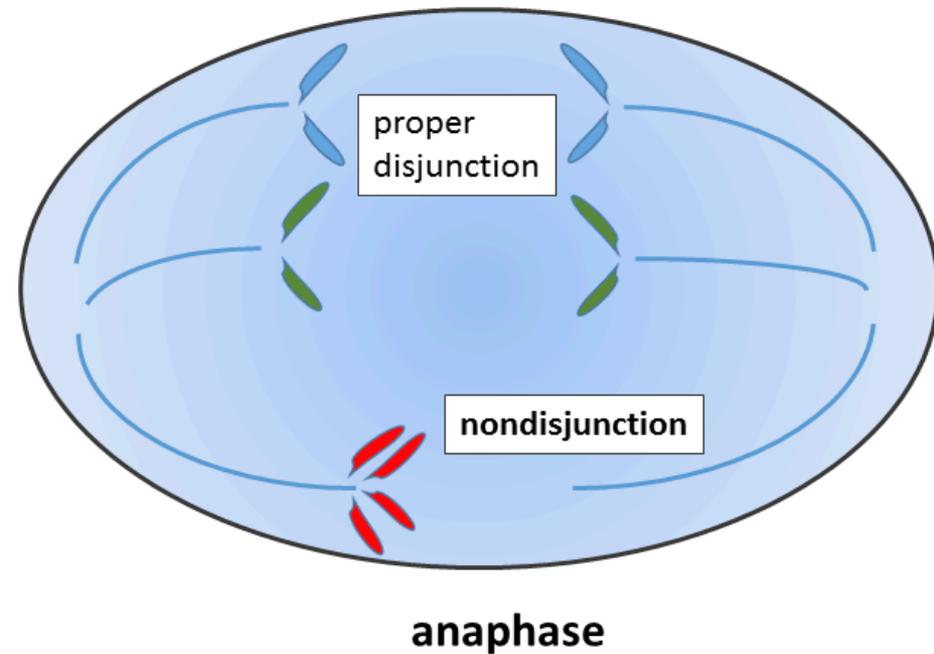
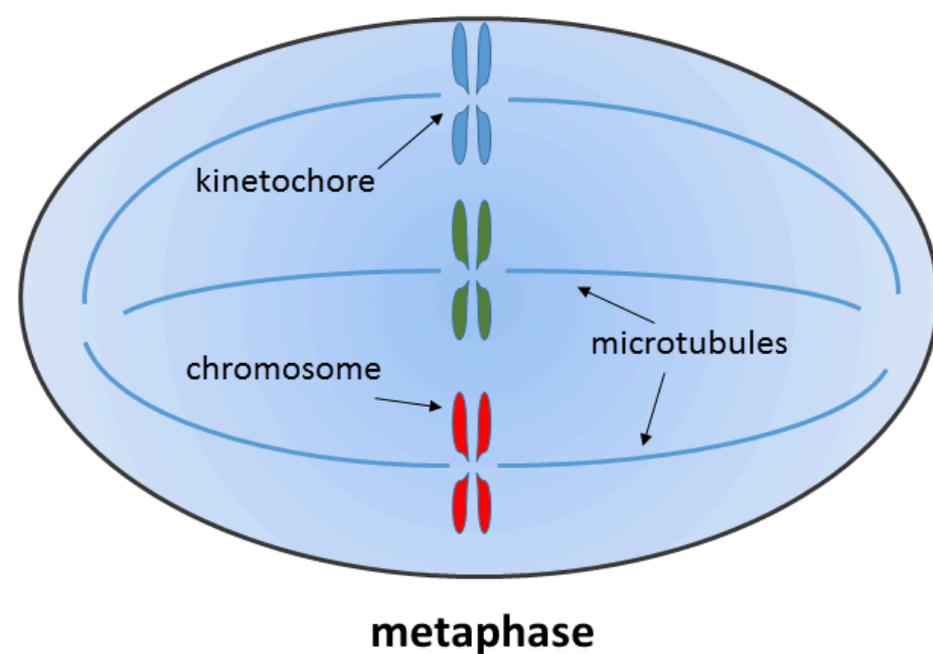
Smith College

Instructor: Prof. Sara Sheehan

# Prenatal Testing Background

# Causes of aneuploidy

↑ abnormal number of chromosomes



# Motivation: aneuploidy testing

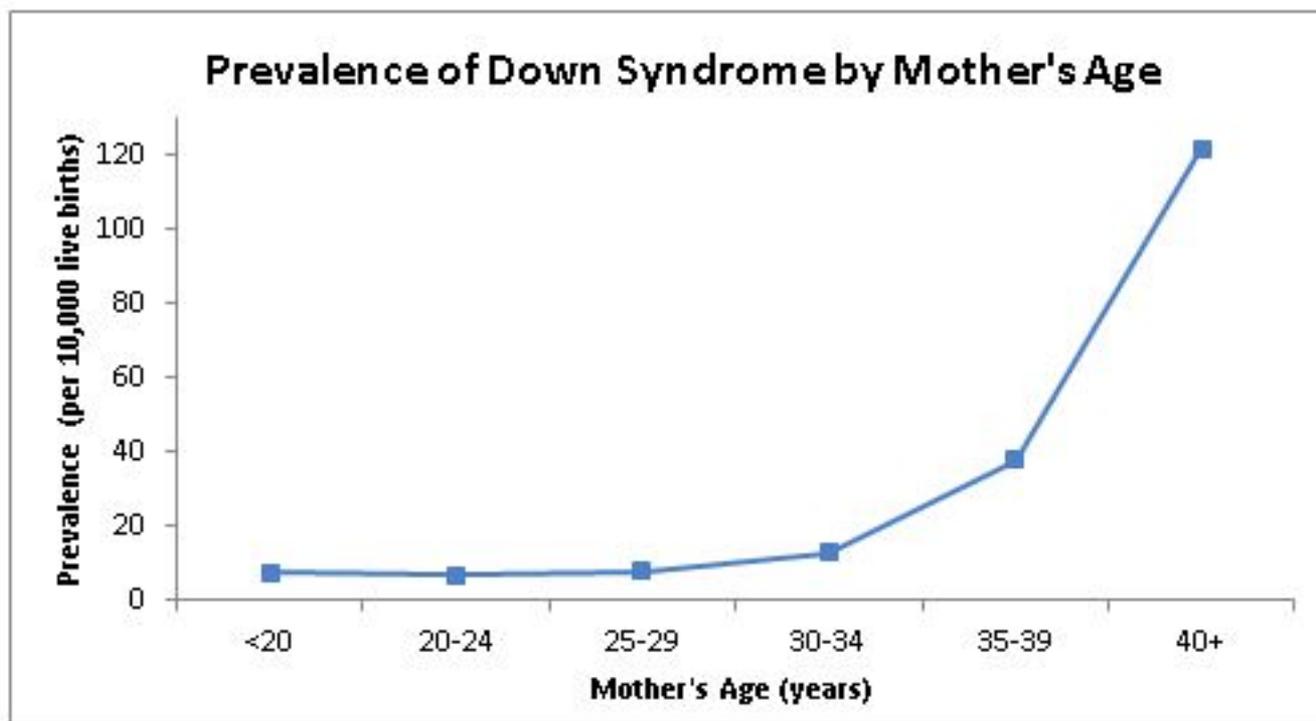
## **Autosomal chromosomes:**

- Trisomy 13: Patau syndrome
- Trisomy 18: Edwards syndrome
- Trisomy 21: Down syndrome

## **Sex chromosomes:**

- X0 (one X chromosome): Turner's syndrome
- XYY or XXX: normal male or female phenotype
- XXY: Klinefelter Syndrome

# Older women are more at risk



# Motivation: aneuploidy testing

- Historically common approach: amniocentesis (invasive)
  - 16-22 weeks
  - serum biochemical assays used as well
- 1981: proof of fetal DNA in maternal blood
  - Y chromosome detected with fluorescence
- ≈2011: companies offer non-invasive prenatal diagnosis
  - Verinata
  - Harmony
  - NIFTY
  - All using next-generation sequencing

# Basic Procedure

- 1) Sample maternal blood
  - contains cell-free fetal DNA (cffDNA)
- 2) Low-coverage sequencing (0.1x - 4x)
- 3) Read alignment/mapping to human genome
  - save reads (“tags”) that map uniquely
- 4) Compute coverage for each chromosome
- 5) *t*-test for aneuploidy (coverage differences)

# Related Work



## Continuous innovation

### Increased safety and peace of mind for your patients

Swift acceptance of the verifi® prenatal test has made a world of difference to high-risk patients across the country:

- **SAFE**—Routine blood draw, **just one tube** (7-10 ml)
- **ACCURATE**—Directly analyzes cell-free fetal DNA with our proprietary SAFer™ algorithm
- **EASY**—Test as early as 10 weeks, no limitations in reference to patient ethnicity, BMI, ART, or egg donor cases
- **FAST**—Results reported in 3-6 business days after sample receipt

### The basic verifi® test detects:

- T21 (Down syndrome)
- T18 (Edwards syndrome)
- T13 (Patau syndrome)

Trisomy 21, 18, 13

### Now a wider option is available for sex chromosomes at no extra charge:

- Monosomy X (MX; Turner syndrome)
- XXX (Triple X)
- XXY (Klinefelter syndrome)
- XYY (Jacobs syndrome)
- **Fetal sex (XX or XY)**—aids in stratifying the risk for X-linked disorders such as hemophilia, Duchenne muscular dystrophy, or cases of ambiguous genitalia, such as congenital adrenal hyperplasia



*t*-test comparing  
chroms 1 and 2:

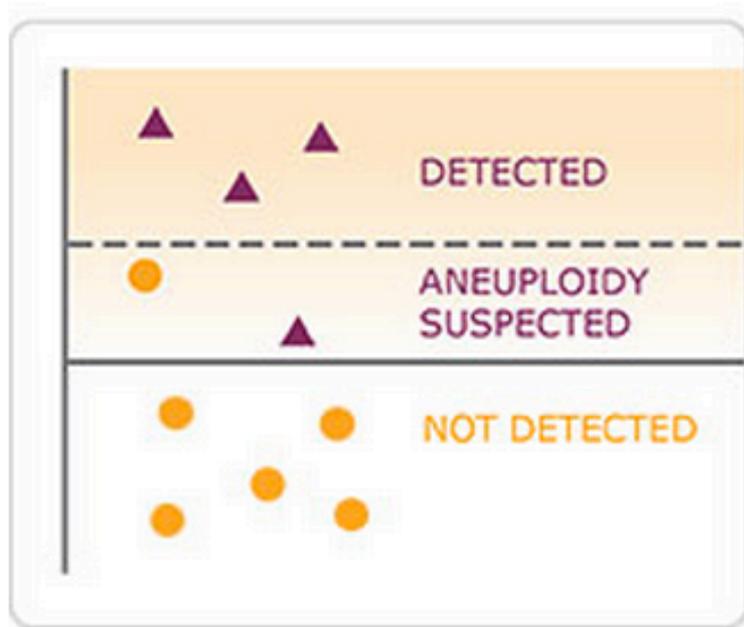
coverage difference  
between two chromosomes

$$t = \frac{\bar{y}_2 - \bar{y}_1}{\sqrt{\frac{s_2^2}{n_2} + \frac{s_1^2}{n_1}}}$$

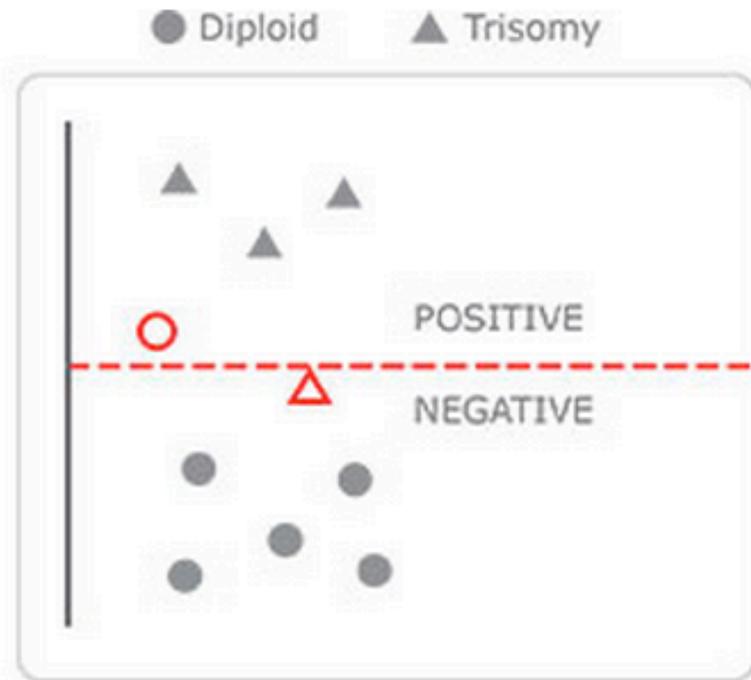
standard deviation

number of windows

threshold for reporting aneuploidy:  $|t| > 3.09$   
(99% confidence interval)



verifi® prenatal test  
Dual Threshold



Single Threshold  
Method

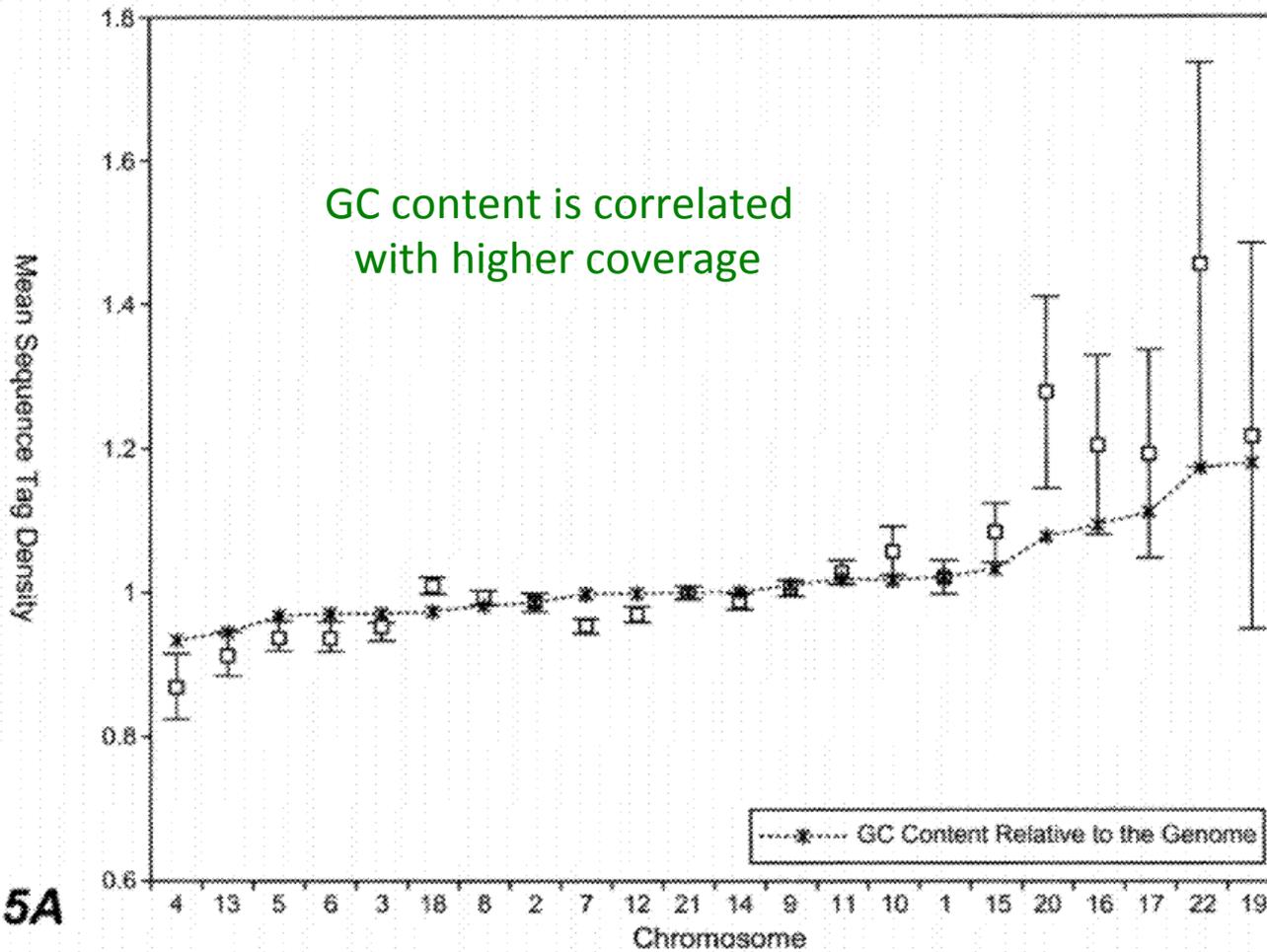


FIG. 5A

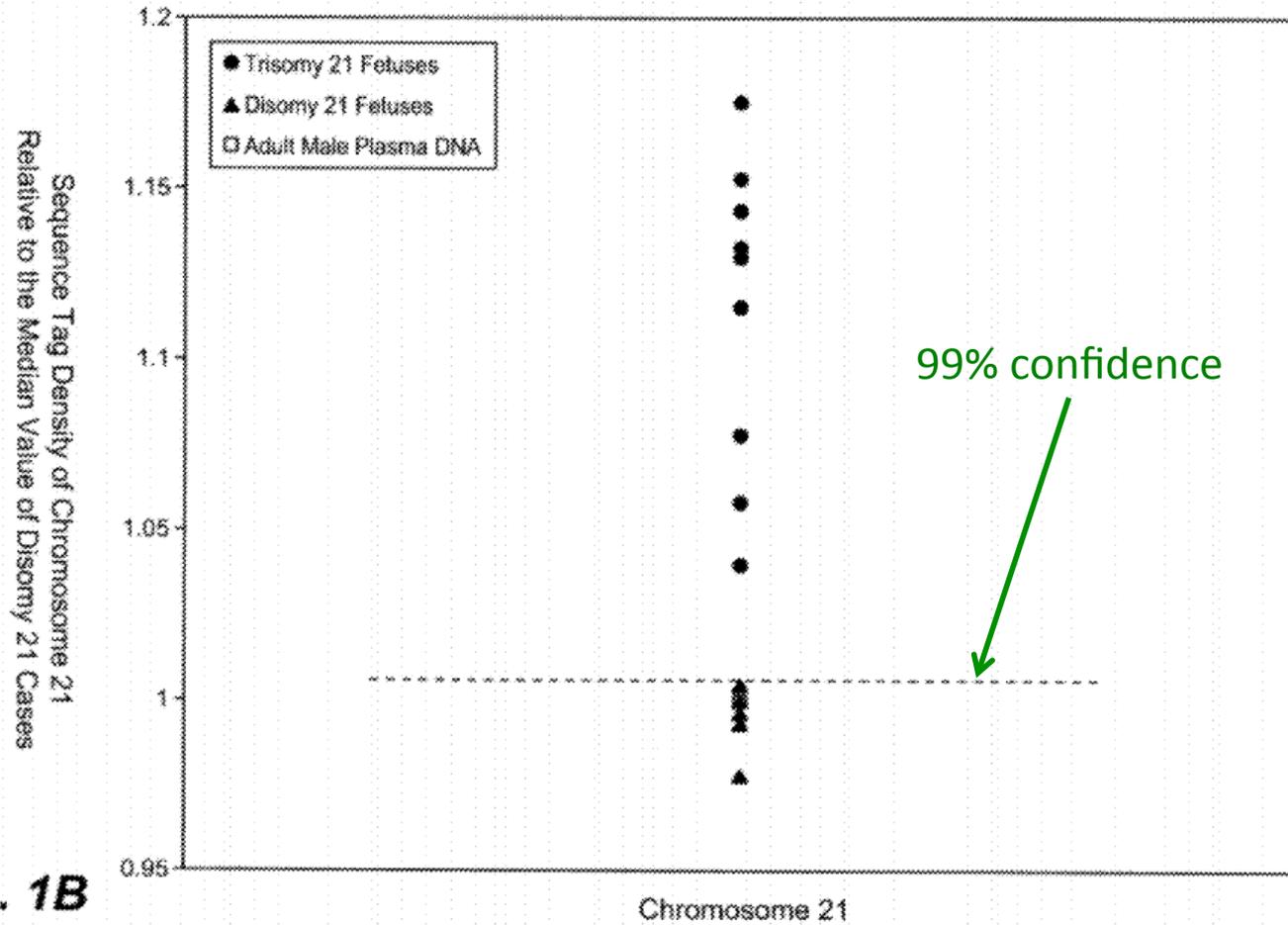
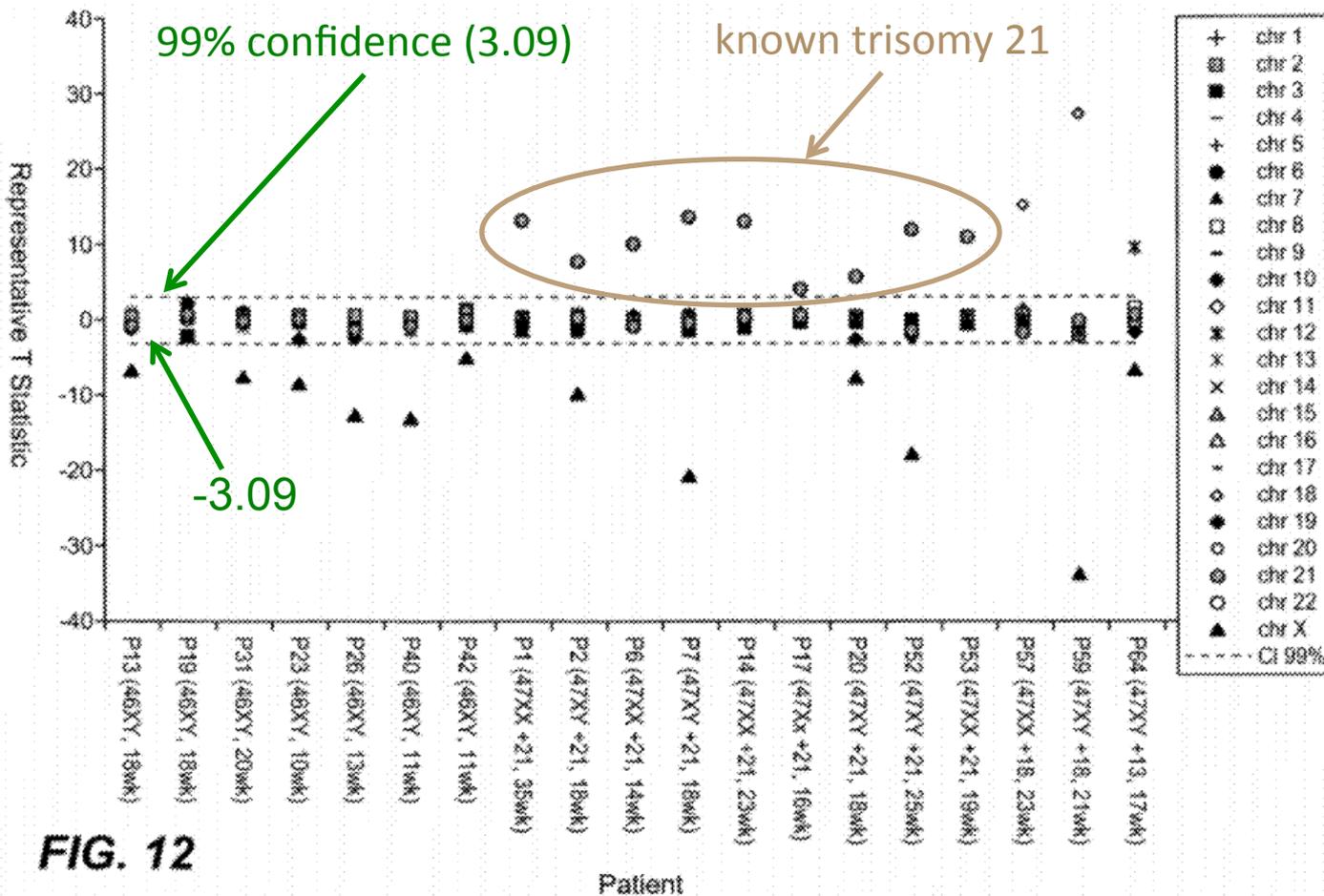


FIG. 1B



**FIG. 12**



## DNA Sequencing versus Standard Prenatal Aneuploidy Screening

Diana W. Bianchi, M.D., R. Lamar Parker, M.D., Jeffrey Wentworth, M.D., Rajeevi Madankumar, M.D., Craig Saffer, M.D., Anita F. Das, Ph.D., Joseph A. Craig, M.D., Darya I. Chudova, Ph.D., Patricia L. Devers, M.S., C.G.C., Keith W. Jones, Ph.D., Kelly Oliver, B.S., Richard P. Rava, Ph.D., and Amy J. Sehnert, M.D. for the CARE Study Group  
N Engl J Med 2014; 370:799-808 | [February 27, 2014](#) | DOI: 10.1056/NEJMoa1311037

	false positive (sequencing)	false positive (standard)	false negative (sequencing)	num positives	PPV (sequencing)	PPV (standard)
T21	0.30%	3.60%	0	5	45.50%	4.20%
T18	0.20%	0.60%	0	2	40.00%	8.30%
T13			0	1		

# NIFTY

- $t$ -test
- critical threshold:  $|t_{i,j,first}| > 3$

$$t_{i,j,first} = \frac{cr_{i,j} - cr'_{i,j}}{sd_j}$$

empirical coverage

expected coverage under null (euploidy)

sample  $i$

chrom  $j$

standard deviation

“Noninvasive Fetal Trisomy (NIFTY) test: an advanced noninvasive prenatal diagnosis methodology for fetal autosomal and sex chromosomal aneuploidies.”

Jiang et al. *BMC Medical Genomics* 2012, 5:57

# NIFTY

## Non-invasive prenatal testing for fetal chromosomal abnormalities by low-coverage whole-genome sequencing of maternal plasma DNA: review of 1982 consecutive cases in a single center

T. K. LAU\*, S. W. CHEUNG†, P. S. S. LO\*, A. N. PURSLEY†, M. K. CHAN‡, F. JIANG‡, H. ZHANG‡, W. WANG‡, L. F. J. JONG\*, O. K. C. YUEN\*, H. Y. C. CHAN\*, W. S. K. CHAN\* and K. W. CHOY§¶

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<i>Chr</i>	<i>Sensitivity</i>	<i>Specificity</i>
21	23/23 (100 (85.7–100))	1959/1959 (100 (99.8–100))
18	4/4 (100 (51.0–100))	1978/1978 (100 (99.8–100))
13	2/2 (100 (34.2–100))	1980/1980 (100 (99.8–100))

Values are given as no. positive/total no. (% (95% CI)).

Chr, chromosome.

# Bayesian Model

# Clinical Trials Example

- Disease affects 1/100 people:  $P(\text{disease}) = 0.01$
- Test for the disease with 90% accuracy
  - $P(\text{positive} | \text{disease}) = 0.9$
  - $P(\text{negative} | \text{healthy}) = 0.9$

$$P(\text{disease} | \text{positive}) = \frac{P(\text{positive} | \text{disease}) P(\text{disease})}{P(\text{positive})}$$

$$\approx 8.3\%$$

# Bayesian Model

Input data are read counts for each chromosome (1,2,...,n):

$$q_1, q_2, \dots, q_n = \vec{q} \qquad \sum_{i=1}^n q_i = N$$

Goal:

$$\begin{aligned} \mathbb{P}(T_{21} | \vec{q}) &= \frac{\mathbb{P}(\vec{q} | T_{21}) \cdot \mathbb{P}(T_{21})}{\mathbb{P}(\vec{q})} \\ &= \frac{\mathbb{P}(\vec{q} | T_{21}) \cdot \mathbb{P}(T_{21})}{\mathbb{P}(\vec{q} | T_{21}) \cdot \mathbb{P}(T_{21}) + \mathbb{P}(\vec{q} | T_{21}^C) \cdot \mathbb{P}(T_{21}^C)} \end{aligned}$$

Prior:

$P(T_{21})$

Maternal Age	Trisomy 21	All Trisomies
20	1 in 1,667	1 in 526
21	1 in 1,429	1 in 526
22	1 in 1,429	1 in 500
23	1 in 1,429	1 in 500
24	1 in 1,250	1 in 476
25	1 in 1,250	1 in 476
26	1 in 1,176	1 in 476
27	1 in 1,111	1 in 455
28	1 in 1,053	1 in 435
29	1 in 1,000	1 in 417
30	1 in 952	1 in 384
31	1 in 909	1 in 384
32	1 in 769	1 in 323
33	1 in 625	1 in 286
34	1 in 500	1 in 238
35	1 in 385	1 in 192
36	1 in 294	1 in 156
37	1 in 227	1 in 127
38	1 in 175	1 in 102
39	1 in 137	1 in 83
40	1 in 106	1 in 66
41	1 in 82	1 in 53
42	1 in 64	1 in 42
43	1 in 50	1 in 33
44	1 in 38	1 in 26
45	1 in 30	1 in 21
46	1 in 23	1 in 16
47	1 in 18	1 in 13
48	1 in 14	1 in 10
49	1 in 11	1 in 8

# Estimating $\epsilon$

(fetal DNA fraction)

- Use Y chromosome
- If trisomy suspected, use extra chrom counts
- Centrifuge maternal DNA
- Look at polymorphism
- Use a constant or don't rely on  $\epsilon$