

Definition: A dissimilarity map on X is a function $\delta : X \times X \rightarrow \mathbb{R}$ with $\delta(x, x) = 0$ and $\delta(x, y) = \delta(y, x)$ for all $x, y \in X$.

Definition: A dissimilarity map δ on X is an ultrametric if for distinct $x, y, z \in X$, $\delta(x, y) \leq \max\{\delta(x, z), \delta(y, z)\}$.

1. The dissimilarity map δ for 5 species, a, b, c, d , and e is shown below. Find an example to show that δ is *not* an ultrametric. Then perform UPGMA to find a tree relating these species. Use the tree to find a new dissimilarity map δ' that *is* an ultrametric.

δ	a	b	c	d	e
a	0	4	6	5	5
b		0	3	5	4
c			0	2	1
d				0	3
e					0